

# Fundamentals of Epidemiology I

## *Measures of Disease Occurrence and Association*

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## Objectives – Day 1

- Review Fundamentals of Epidemiology
  - Measures of Disease Occurrence and Association
  - Study Designs
  - Epidemiologic Concepts
    - Bias
    - Confounding
    - Random Variation
  - Group Exercise

## Measures of Disease Occurrence

PREVALENCE =  $\frac{\text{NUMBER OF EXISTING CASES OF A DISEASE}}{\text{TOTAL STUDY POPULATION AT THAT TIME}}$

*Synonym(s): Prevalence rate*

*Notes: Prevalence is not a rate, it is a unitless proportion.  
It takes on values from 0 to 1 (e.g. 0.2, 0.7)  
Can be thought of as a %*

*Not a measure of new cases, but all cases  
Prevalence a function of incidence rate and disease duration*

*Example:* Among a sample of men aged 50-80 years in Bangkok, 30 of 2400 men examined in 1986 had cancer

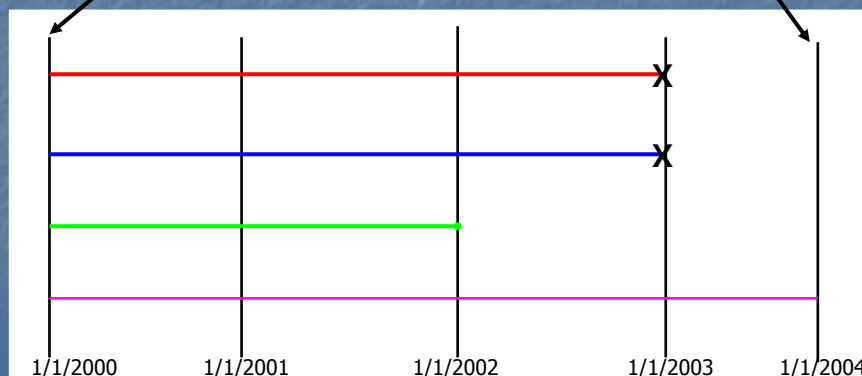
$$\text{Prevalence} = 30/2400 = 0.0125 * 100 = 1.25\%$$

$$\text{RISK} = \frac{\text{NUMBER OF NEW CASES OF DISEASE FROM } T_0 \text{ TO } T_1}{\text{NUMBER OF SUBJECTS AT RISK AT } T_0}$$

$$= \frac{2}{4} = 0.50 * 100\% = 50\%$$

$T_0$  = start of follow-up

$T_1$  = end of follow-up



## RISK

*Synonym(s): Cumulative incidence, incidence proportion*

*Notes: Individual's probability of developing disease over specified time period*

*A unitless proportion, not a rate*

*It takes on values from 0 to 1 (e.g. 0.2, 0.7)*

*Can be thought of as a %*

*Measure of new cases in a population of previously disease free subjects*

*Example:* Among a sample of men aged 50-80 years in Bangkok, 2370 men of 2400 examined in 1986 were free of cancer.

From 1986 to 2006, 150 of them developed cancer.

$$\text{Risk} = 150/2370 = 0.021 * 100 = 2.1\%$$

# Problems with Risk

- **Competing risks**

Subjects may die of other disease early during the study, and thus cannot develop disease of interest. They cannot contribute to numerator. Yet, they contribute to denominator.

- **Loss to follow-up**

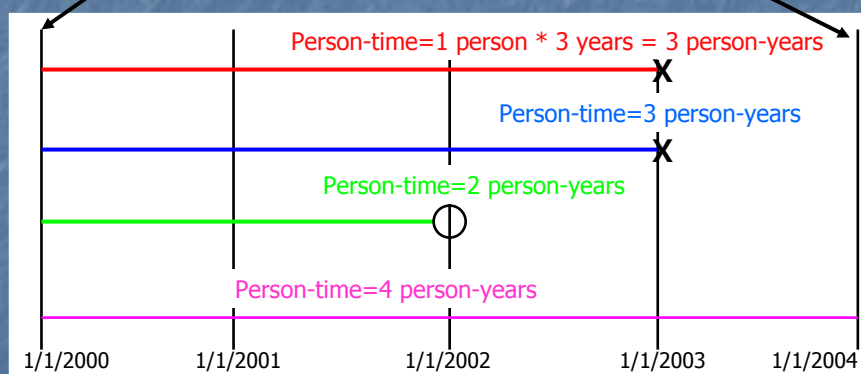
Subjects may move out of study area, or become non-responsive, and thus we do not know if they developed disease or not. Therefore, they cannot contribute to the numerator, but they do contribute to the denominator.

$$\text{Incidence rate} = \frac{\text{Number of events that occur from } T_0 \text{ to } T_1}{\text{Total person-time of observation}}$$

Person-time = Sum of total time spent in study for all study subjects

$T_0$  = start of follow-up

$T_1$  = end of follow-up



$$\text{Total person-time} = 3 + 3 + 2 + 4 \text{ person-years} = 12 \text{ person-years}$$

## INCIDENCE RATE

*Synonym(s): Hazard rate*

*Notes: # new cases occurring in population per unit of person-time  
Has units (i.e. "person-time"), is a rate  
Takes on values from 0 to  $\infty$*

*Example:* Among a sample of men aged 50-80 years in Bangkok, 2370 men of 2400 examined in 1986 were free of cancer. From 1986 to 2006, each subject was followed for 20 years, and 150 men developed cancer.

$$\begin{aligned}\text{Incidence rate} &= 150 / (2370 \text{ persons} * 20 \text{ years}) \\ &= 0.0032 \text{ cases of cancer/1 person-year} \\ &= 3.2 \text{ cases of cancer/1000 person-years}\end{aligned}$$

- Prevalence is a function of both incidence rate and duration  
$$\frac{\text{Prevalence}}{1 - \text{Prevalence}} = \text{Incidence Rate} * \text{Duration}$$

*Example:*

Prevalence=5%

Incidence rate=10 cases of disease/10 person-years

**Duration = ? years**

$$\frac{0.05}{(1-0.05)} = \frac{10 \text{ cases}}{10 \text{ person-years}} * \text{Duration years}$$

**Duration = 0.52 years**

- If prevalence < 0.10 or 10% then:  
Prevalence  $\sim$  Incidence Rate \* Duration

$$0.05 = \frac{10 \text{ cases}}{10 \text{ person-years}} * \text{Duration years}$$

**Duration = 0.5 years**



## Measures of Disease Association

$$\text{Rate Ratio} = \text{IR}_{\text{Exposed}} / \text{IR}_{\text{Unexposed}}$$

*Synonym: Relative risk*

*Notes: Ranges from 0 to  $\infty$   
When no association between exposure and disease,  $RR=1$   
 $RR < 1$  indicates exposure decreases incidence rate  
 $RR > 1$  indicates exposure increases incidence rate  
All ratio measures are unitless*

<i>Example:</i>	Radiation	No Radiation
Breast cancer cases	41	15
Person-years	28,010	19,017

$$RR = (41/28,010 \text{ PY}) / (15/19,017 \text{ PY}) = 1.85$$

Radiation exposure results in an **85% increase in the incidence rate of breast cancer**, compared to no radiation exposure.

$$\text{Risk Ratio} = \text{Risk}_{\text{Exposed}} / \text{Risk}_{\text{Unexposed}}$$

*Synonyms: Cumulative incidence ratio, relative risk*

*Notes:*

- Ranges from 0 to  $\infty$*
- When no association between exposure and disease,  $RR=1$*
- $RR < 1$  indicates exposure is protective*
- $RR > 1$  indicates exposure increases risk*
- All ratio measures are unitless*

<i>Example:</i>	Radiation	No Radiation
Breast cancer cases	41	15
Non-breast cancer	17	27
Subjects at risk	58	42

$$RR = (41/58) / (15/42) = 1.98$$

Subjects with radiation exposure have 98% greater risk of developing breast cancer, than subjects without radiation exposure.

$$\text{Rate Difference} = \text{IR}_{\text{Exposed}} - \text{IR}_{\text{Unexposed}}$$

*Notes:* Ranges from  $-\infty$  to  $+\infty$   
 When no association between exposure and disease,  $\text{RD}=0$   
 $\text{RD} < 0$  indicates exposure decreases incidence rate  
 $\text{RD} > 0$  indicates exposure increases incidence rate  
 $\text{RD}$  is in units of person-time

*Example:*

	Radiation	No Radiation
Breast cancer cases	41	15
Person-years	28,010	19,017

$$\begin{aligned} \text{RD} &= (41/28,010 \text{ PY}) - (15/19,017 \text{ PY}) = 0.000675 \text{ cases/1 PY} \\ &= 6.75 \text{ cases/10,000 person-years} \end{aligned}$$

Radiation exposure results in an increase of 6.75 breast cancer cases/10,000 person-years, compared to no radiation exposure.

$$\text{Risk Difference} = \text{Risk}_{\text{Exposed}} - \text{CI}_{\text{Unexposed}}$$

*Synonyms:* Attributable risk, attributable risk among the exposed

*Notes:* Ranges from  $-1$  to  $+1$   
 When no association between exposure and disease,  $\text{RD}=0$   
 $\text{RD} < 0$  indicates exposure decreases risk  
 $\text{RD} > 0$  indicates exposure increases risk  
 unitless

*Example:*

	Radiation	No Radiation
Breast cancer cases	41	15
Non-breast cancer	17	27
Subjects at risk	58	42

$$\text{RD} = (41/58) - (15/42) = 0.35 * 100\% = 35\%$$

There is a 35% increase in the risk of breast cancer associated with radiation exposure, compared to the risk found in subjects without radiation exposure.



$$\text{Attributable Risk \%} = ((RR - 1) / RR) * 100$$

*Synonyms:* Etiologic fraction, relative excess incidence, attributable proportion

*Notes:* Fraction of disease burden among the exposed that can be attributed to exposure.

*Example:*

	Radiation	No Radiation
Breast cancer cases	41	15
Non-breast cancer	17	27
Subjects at risk	58	42

$$RR = (41/58) / (15/42) = 1.98$$

$$AR\% = (1.98 - 1) / 1.98 * 100 = 49\%$$

Approximately 49% of the breast cancer risk in those exposed to radiation is due to radiation exposure.

### Population Attributable Risk %

$$PAR\% = ((Risk_{TOTAL} - Risk_{Unexposed}) / Risk_{TOTAL}) * 100$$

*Notes:* Fraction of disease in the population that is attributable to exposure, and thus could be eliminated if exposure were eliminated

*Example:*

	Radiation	No Radiation	Total
Breast cancer cases	41	15	56
Non-breast cancer	17	27	44
Subjects at risk	58	42	100

$$PAR\% = ((56/100) - (15/42)) / (56/100) * 100 = 36\%$$

Approximately 36% of new breast cancer cases would be eliminated in this population if radiation exposure was eliminated

- **Note:** The principles and interpretation of attributable rate percent, and population attributable rate are similar to those given for risks
- They are just calculated with incidence rates rather than risks

### Odds Ratio = $ad/bc$

Used in both case-control and cohort studies

Due to common use of logistic regression

Used to approximate the rate ratio or risk ratio

	Exposed	Unexposed
Disease	a	b
No Disease	c	d

## Review/Examples

- If we want to quantify # of existing cases in the population
  - Prevalence =  $\frac{\text{\# of existing cases of disease}}{\text{\# of people in the population}}$
- If we want to quantify the # of new cases in a population
  - Risk =  $\frac{\text{\# of new cases of disease since } T_0}{\text{\# of people at risk in the population at } T_0}$
  - Incident Rate =  $\frac{\text{\# of new cases of disease since } T_0}{\text{\# of person-years accrued by population at risk since } T_0}$

## Review/Examples

- If you want to compare the burden of disease in an exposed population to that of an unexposed population.

*Is exposure associated with a greater/lower risk/rate of disease?*

$$\text{Rate Ratio (RR)} = \text{IR}_{\text{Exposed}} / \text{IR}_{\text{Unexposed}}$$

$$\text{Risk Ratio (RR)} = \text{Risk}_{\text{Exposed}} / \text{Risk}_{\text{Unexposed}}$$

$$\text{Odds Ratio (OR)} = ad/bc$$

	Exposed	Unexposed
Disease	a	b
No Disease	c	d

$$\text{Rate Difference} = \text{IR}_{\text{Exposed}} - \text{IR}_{\text{Unexposed}}$$

$$\text{Risk Difference} = \text{Risk}_{\text{Exposed}} - \text{Risk}_{\text{Unexposed}}$$

# Harvard Six Cities Mortality Study

*Dockery et al, NEJM 1993*

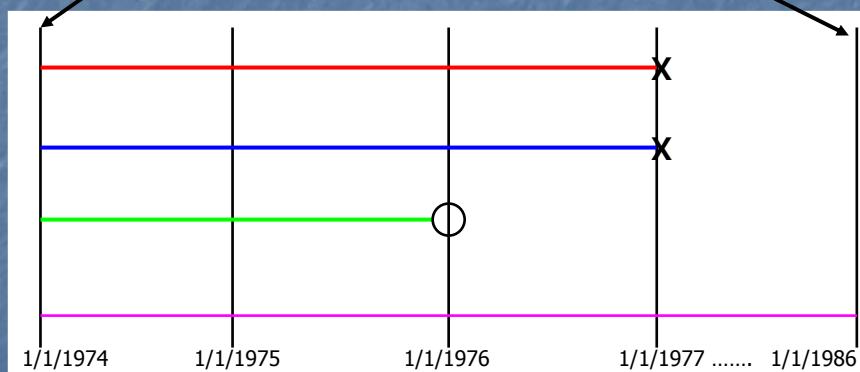
- Prospective study of effects of air pollution on respiratory disease
- 8111 subjects randomly selected 1974-77 in six communities
- Questionnaire on risk factors for respiratory disease, PF test
- Mortality follow-up through 1989
- Cities selected to represent range of exposures to air pollution from fossil fuels
- Community air monitors in each city
  - TSP, PM<sub>10</sub>, PM<sub>2.5</sub>, SO<sub>4</sub>
  - SO<sub>2</sub>, NO<sub>2</sub>, O<sub>3</sub>

Incidence rate =  $\frac{\text{Number of events that occur from } T_0 \text{ to } T_1}{\text{Total person-time of observation}}$

Person-time = Sum of total time spent in study for all study subjects

$T_0$  = start of follow-up

$T_1$  = end of follow-up



Calculate **incident mortality** with person-years denominator

	Deaths		Person-Years	Deaths/1000 p-yrs	Relative Risk (95% CI)
	Yes	No			
Portage, WI	232	-	21,618	10.73	1.00
Topeka, KS	156	-	16,111	9.68	0.90 ( 0.74 , 1.11 )
Watertown, MA	248	-	19,882	12.47	1.16 ( 0.97 , 1.39 )
Harriman, TN	222	-	17,836	12.45	1.16 ( 0.96 , 1.39 )
St.Louis, MO	281	-	17,715	15.86	1.48 ( 1.24 , 1.76 )
Steubenville,OH	291	-	17,914	16.24	1.51 ( 1.27 , 1.80 )
	1430		111,076		

Next:

Epidemiologic Study  
Designs